

483. Umnožak nultočaka funkcije $f(x) = \frac{3x-1}{x+3} - \frac{x+3}{3x-1} - \frac{3}{2}$ je jednak:

1. -1 2. 1 3. -3 4. 3

$$f(x) = \frac{3x-1}{x+3} - \frac{x+3}{3x-1} - \frac{3}{2}$$

$$\frac{3x-1}{x+3} = t \quad \text{supstitucija}$$

$$t - \frac{1}{t} - \frac{3}{2} = 0 / \cdot 2t$$

$$2t^2 - 2 - 3t = 0$$

$$2t^2 - 3t - 2 = 0 \quad \text{kvadratna jednažba}$$

$$t_{1/2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{3 \pm \sqrt{9 + 4 \cdot 2 \cdot 2}}{2 \cdot 2} = \frac{3 \pm \sqrt{9 + 16}}{4} = \frac{3 \pm \sqrt{25}}{4}$$

$$= \frac{3 \pm 5}{4}$$

$$t_1 = 2 \quad t_2 = -\frac{2}{4}$$

$$t_2 = -\frac{1}{2}$$

$$\frac{3x-1}{x+3} = 2 / \cdot (x+3)$$

$$3x-1 = 2(x+3)$$

$$3x-1 = 2x+6$$

$$3x-2x = 6+1$$

$$x_1 = 7$$

$$\frac{3x-1}{x+3} = -\frac{1}{2} / \cdot 2(x+3)$$

$$2(3x-1) = -(x+3)$$

$$6x-2 = -x-3$$

$$6x+x = 2-3$$

$$7x = -1 / :7$$

$$x_2 = -\frac{1}{7}$$

$$x_1 \cdot x_2 = 7 \cdot \left(-\frac{1}{7}\right) = -1$$